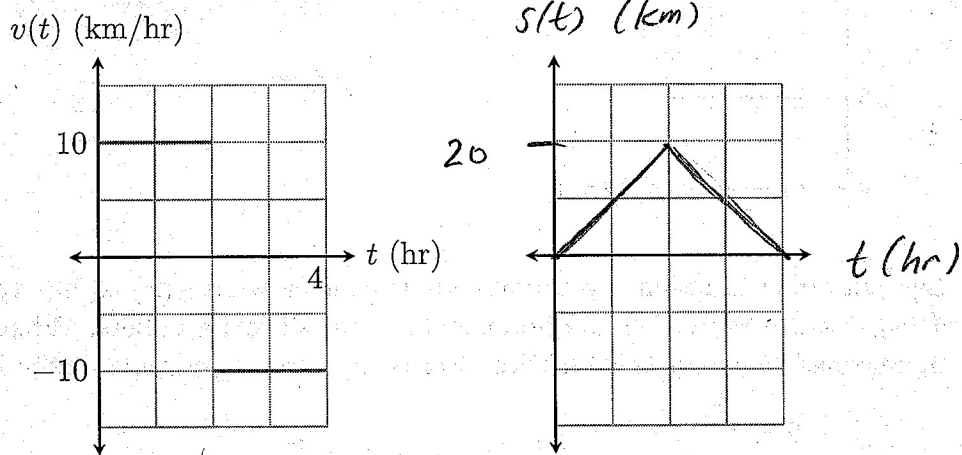


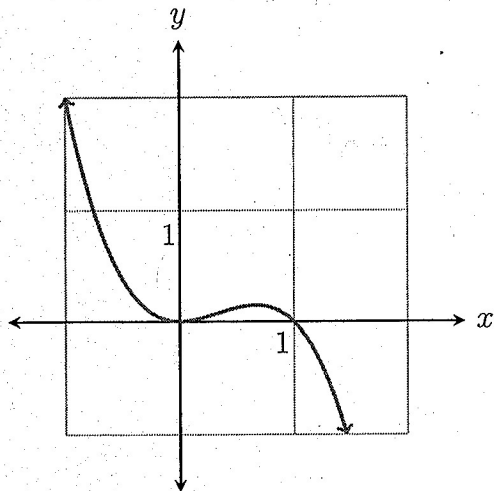
1. You are given a velocity graph below. Draw the corresponding displacement graph on the blank grid. Label axes carefully!



Write a brief sentence describing this journey.

You drive 2 hours east at 10 km/hr, then you turn around and drive 2 hours west at 10 km/hr

2. Below is a graph of the function $f(x) = x^2 - x^3$. Find an equation of the tangent line in the form $y = mx + b$ at $x = 1$. You can use the graph to verify your answer, but you have to use calculus to find the equation.



$$f'(x) = 2x - 3x^2$$

$$m = f'(1) = 2(1) - 3(1)^2 = -1$$

$$\text{point: } f(1) = 1^2 - 1^3 = 0$$

$$(1, 0)$$

$$y = mx + b$$

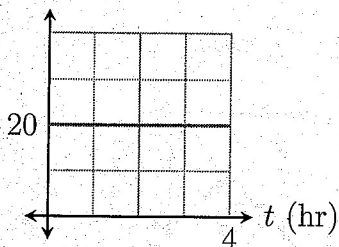
$$0 = -1(1) + b$$

$$b = 1$$

$$y = -x + 1$$

3. Below is a graph of a velocity curve. Find an equation for the displacement curve.

$v(t)$ (km/hr)



$$s(t) = \text{area under } v(t) \\ = 20t$$

4. Let $f(x)$ be a function – you don't know exactly what $f(x)$ is, but you are given that $f'(x) = x(3 - 2x)^2$. The function is defined on all real numbers. Where is this function increasing? Where is this function decreasing? Write your answers in interval notation.

$(3 - 2x)^2$ is always positive.

So $f'(x) < 0$ when $x < 0$, and $f'(x) > 0$ when $x > 0$.

Increasing: $(0, \infty)$

Decreasing: $(-\infty, 0)$

5. Find the derivatives of the following functions.

(a) $h(x) = \frac{7}{x^2} = 7x^{-2}$

$$h'(x) = 7(-2x^{-3}) = -14x^{-3}$$

(b) $h(x) = 3x \cos(x)$

$$f(x) = 3x \quad f'(x) = 3$$

$$g(x) = \cos(x) \quad g'(x) = -\sin(x)$$

$$f(x)g'(x) + g(x)f'(x)$$

$$3x(-\sin(x)) + \cos(x) \cdot 3$$

$$-3x \sin(x) + 3 \cos(x)$$

$$(c) h(x) = \frac{2x}{\sin(x)}$$

$$f(x) = 2x \quad f'(x) = 2$$

$$g(x) = \sin(x) \quad g'(x) = \cos(x)$$

$$\frac{g(x)f'(x) - f(x)g'(x)}{g(x)^2}$$

$$\frac{\sin(x) \cdot 2 - 2x \cdot \cos(x)}{(\sin(x))^2} = \frac{2 \sin(x) - 2x \cos(x)}{\sin^2(x)}$$

$$(d) h(x) = \cos(5x^2)$$

$$f(x) = \cos(x) \quad f'(x) = -\sin(x)$$

$$g(x) = 5x^2 \quad g'(x) = 10x$$

$$f'(g(x))g'(x)$$

$$-\sin(g(x)) \cdot 10x$$

$$-10x \sin(5x^2)$$

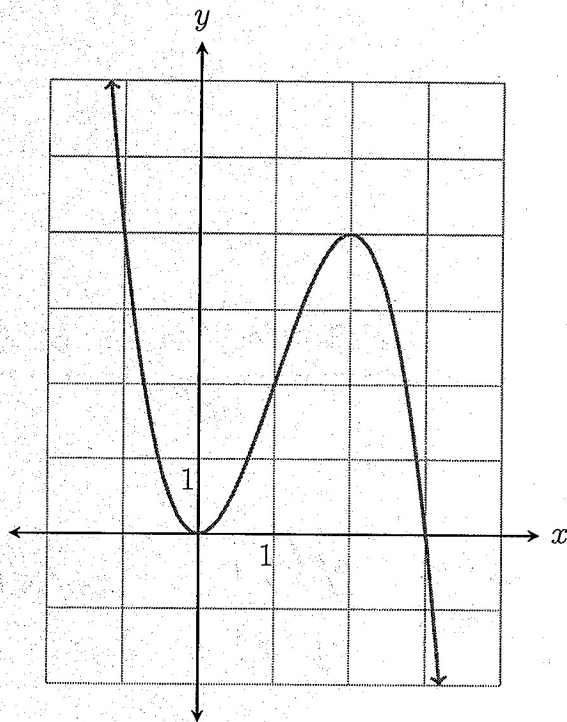
6. Suppose $f(x) = 3x - \cos(x)$. Find $f''(x)$.

$$f'(x) = 3 - (-\sin(x))$$

$$= 3 + \sin(x)$$

$$f''(x) = \cos(x)$$

7. Below is a graph of $f(x) = 3x^2 - x^3$. You are given that $f'(x) = 6x - 3x^2$ and $f''(x) = 6 - 6x$. By making the appropriate sign chart, find all inflection points on this curve.



$$f''(x) = 6 - 6x = 0$$



Test points:

$$f''(-1) = 6 - 6(-1) = 12 > 0$$

$$f''(2) = 6 - 6 \cdot 2 = -6 < 0$$

Since concavity changes at $x=1$, there is an inflection point at $(1, 2)$.

8. Fill in the blank with the best answer. Write out words completely; do not use abbreviations.

- (a) We use information about when $f'(x)$ is positive or negative to determine where the function is increasing or decreasing.
- (b) We use information about when $f''(x)$ is positive or negative to determine where the function is concave up or concave down.
- (c) An inflection point is a point on the graph where the concavity changes.